

Zero-Aware Pattern Databases with 1- Bit Compression for Sliding Tile Puzzles

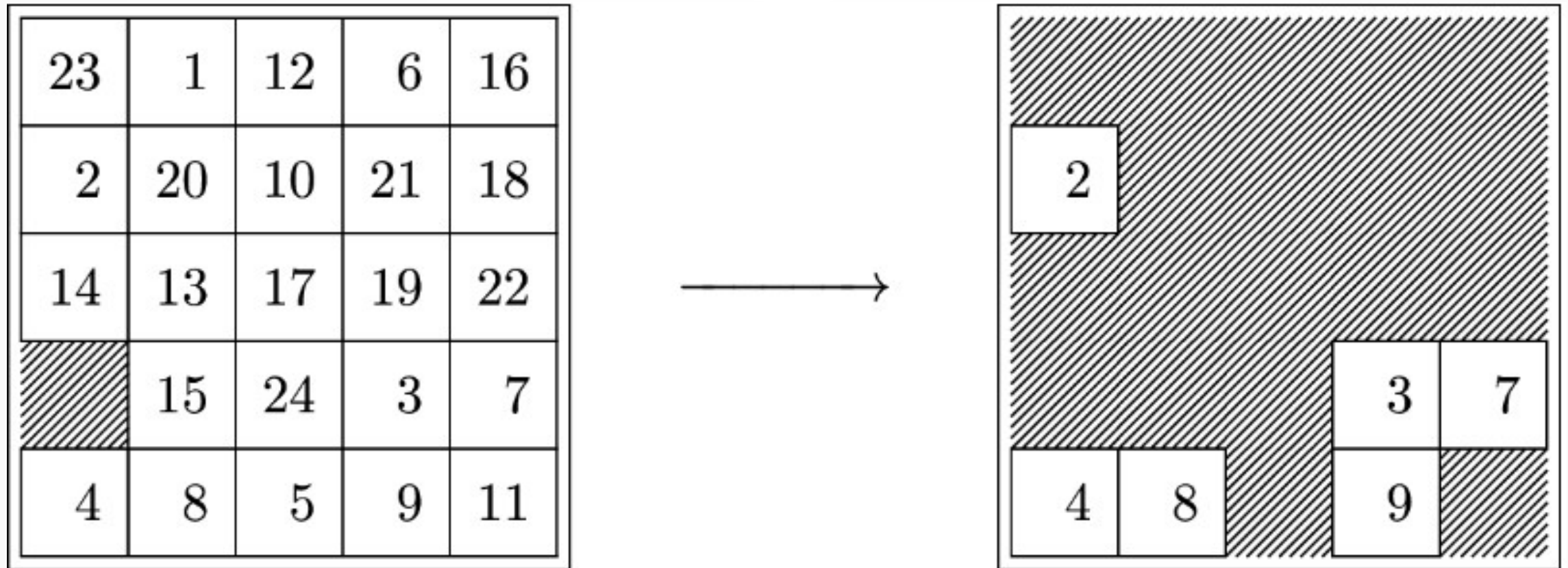
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motivation

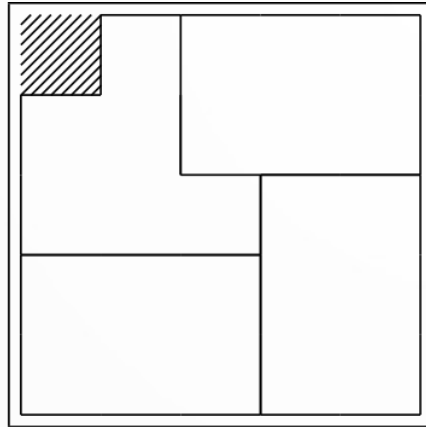
- sliding tile puzzles are a testbed problem for heuristic search
- currently best known heuristics:
additive pattern databases (APDBs)
- can we do better?

additive pattern databases

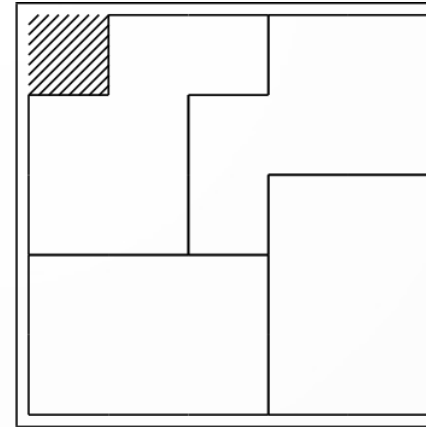


a 24 puzzle and its $\{2, 3, 4, 7, 8, 9\}$ APDB

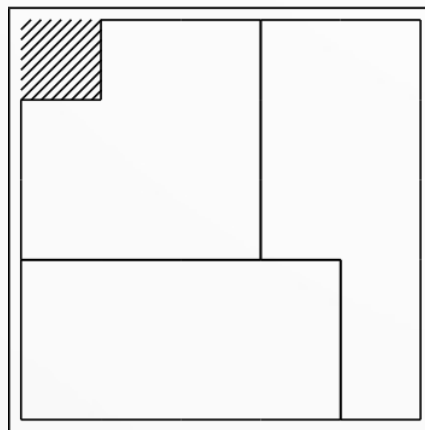
additive pattern databases



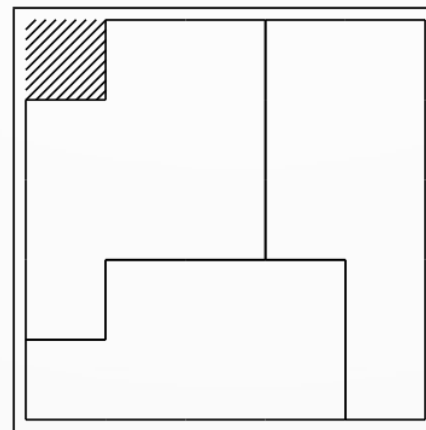
6-6-6-6 orig.



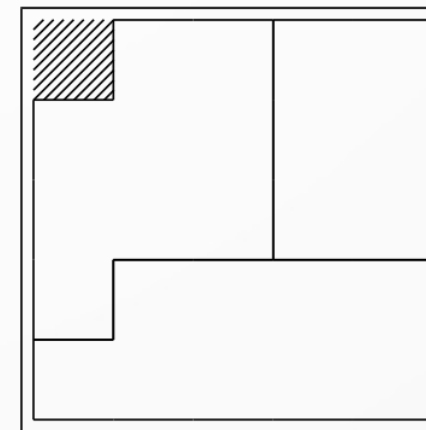
6-6-6-6 new



8-8-8



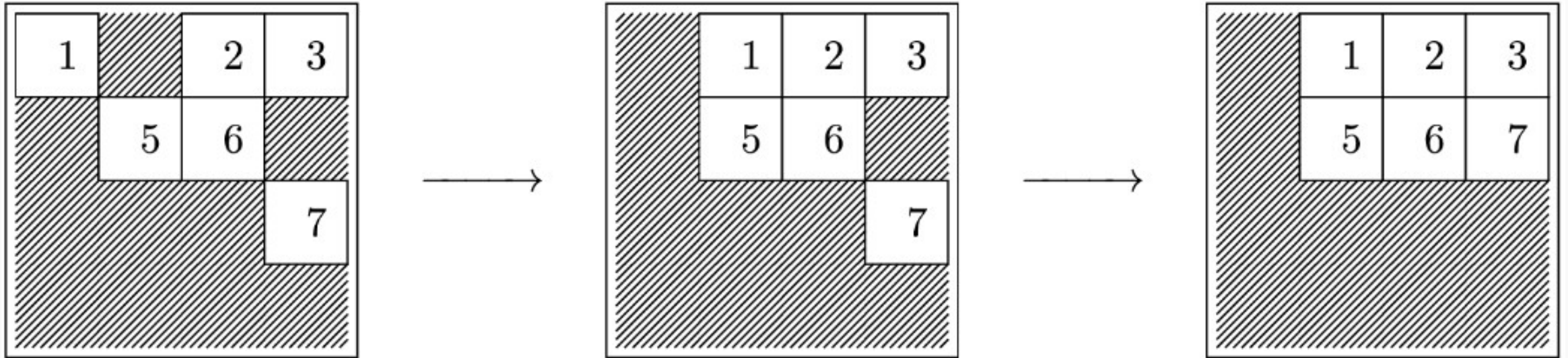
9-8-7



9-9-6

some partitionings of the 24-puzzle

limitations



$h = 2$ is predicted by the APDB but 2 moves are not sufficient

tracking the blank (zero tile)

| | | | |
|----|----|----|----|
| 1 | 3 | 8 | 9 |
| 10 | 6 | | 4 |
| 2 | 12 | 5 | 15 |
| 14 | 7 | 13 | 11 |

(a)

| | | | |
|---|---|---|---|
| 1 | 3 | | |
| | 6 | | 4 |
| 2 | | 5 | |
| | 7 | | |

(b)

| | | | |
|---|---|---|---|
| ○ | ○ | A | A |
| B | ○ | A | ○ |
| ○ | C | ○ | D |
| E | ○ | D | D |

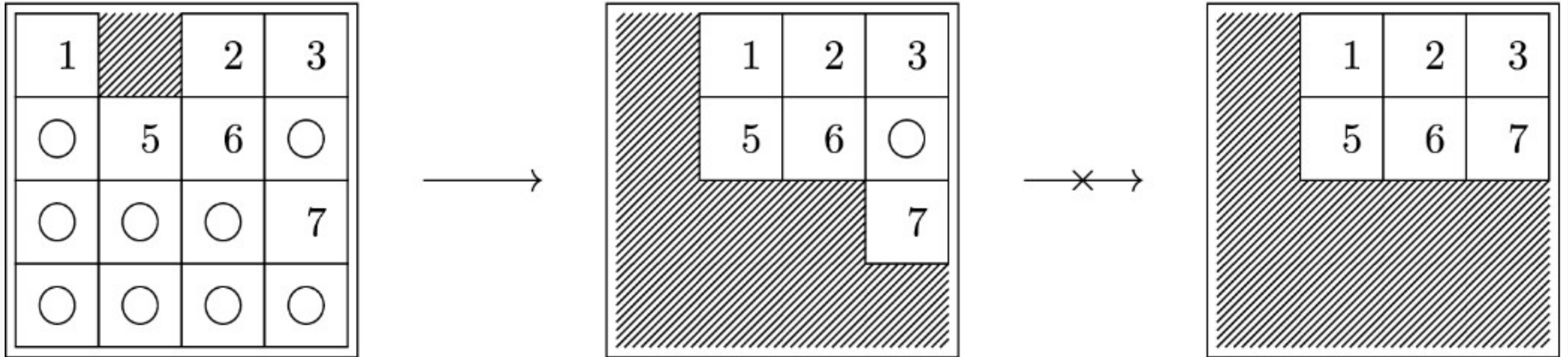
(c)

| | | | |
|---|---|---|---|
| 1 | 3 | | |
| ○ | 6 | | 4 |
| 2 | ○ | 5 | ○ |
| ○ | 7 | ○ | ○ |

(d)

- (a) a configuration of the 15 puzzle
- (b) as seen by the $\{1, 2, 3, 4, 5, 6, 7\}$ APDB
- (c) its possible zero-tile regions A–E
- (d) as seen by the $\{1, 2, 3, 4, 5, 6, 7\}$ ZPDB

limitations revisited

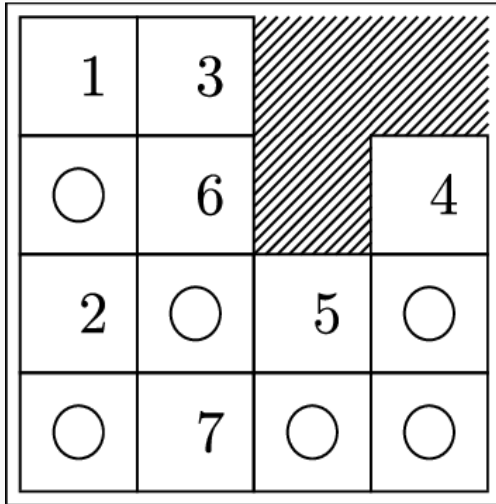


the ZPDB does not predict a 2 move solution

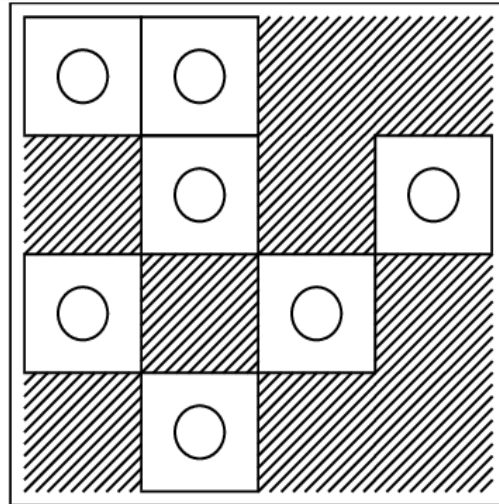
space considerations

| k | APDB size | ZPDB size | avg | max |
|-----|-----------------------|-----------------------|------|-----|
| 2 | 600 | 608 | 1.01 | 2 |
| 3 | 13 800 | 14 472 | 1.04 | 2 |
| 4 | 303 600 | 339 048 | 1.12 | 3 |
| 5 | 6 375 600 | 7 871 280 | 1.23 | 4 |
| 6 | 127 512 000 | 181 008 000 | 1.42 | 5 |
| 7 | 2 422 728 000 | 4 066 655 040 | 1.68 | 6 |
| 8 | 43 609 104 000 | 87 358 400 640 | 2.00 | 7 |
| 9 | 741 354 768 000 | 1 759 513 674 240 | 2.37 | 8 |
| 10 | 11 861 676 288 000 | 32 787 717 580 800 | 2.76 | 10 |
| 11 | 177 925 144 320 000 | 560 680 553 664 000 | 3.15 | 11 |
| 12 | 2 490 952 020 480 000 | 8 749 801 518 796 800 | 3.51 | 13 |

representation



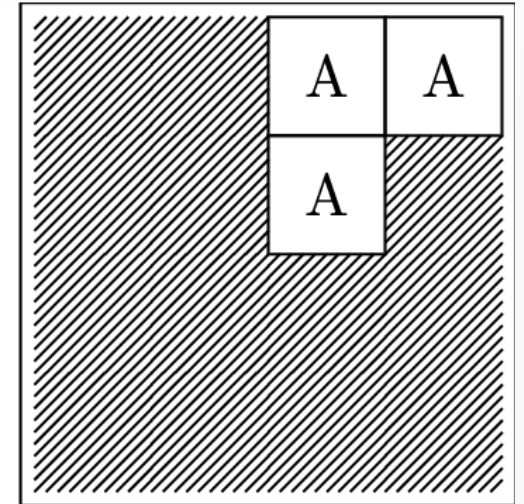
$e = (m, p, r)$



$m = 2027$

$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 1 & 3 & 6 & 4 & 2 & 5 & 7 \end{pmatrix}$

$p = 198$



$r = 0$

*representing a ZPDB entry by tile **m**ap, **p**ermutation,
and zero tile **r**egion*

enhanced compression

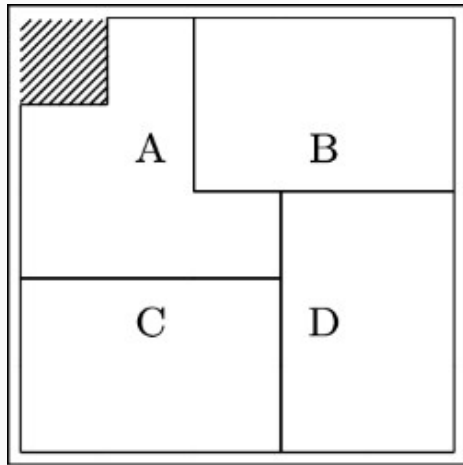
- ZPDBs heuristics are consistent with unit weight
- the difference between adjacent h -values is ± 1
- knowing the change of h -value is sufficient for search
- [Breyer2010a] represented PDB entries mod 3 in $\log_2 3 \approx 1.6$ bits per entry using this idea.
- but we can do better
 - if we store entries mod 4, we need 2 bits per entry
 - the least bit can be omitted for bipartite spaces
 - giving us a representation with 1 bit per entry

building collections

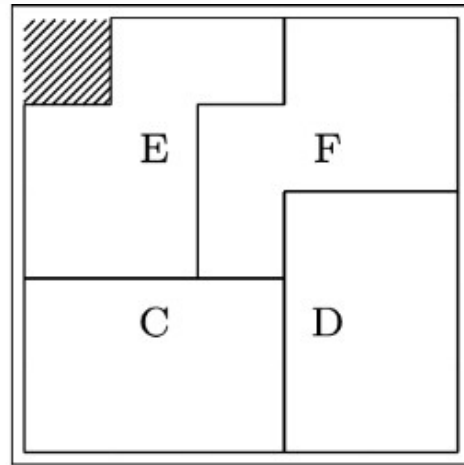
the general approach:

1. start with a set of known good partitionings
2. sample the h -values of $n = 10^8$ random puzzles
3. for each partitioning, count how often it was an h -values sole support
4. remove partitionings from the collection which rarely supported the maximum h -value
5. add new partitionings to replace them
6. repeat steps 2–5 until no improvements are found

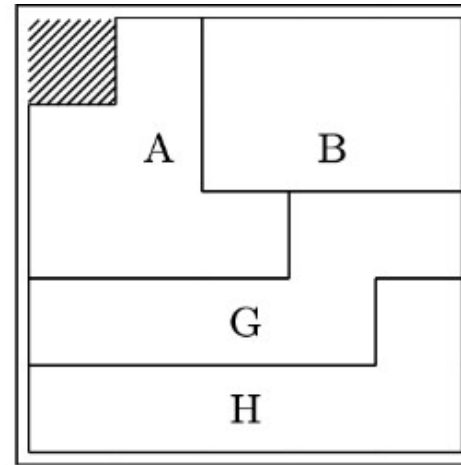
building collections



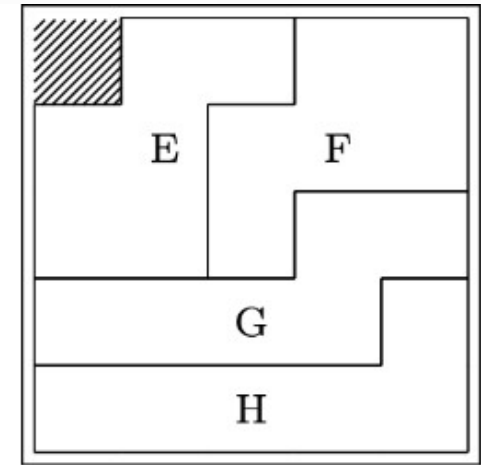
(a) 2.21%



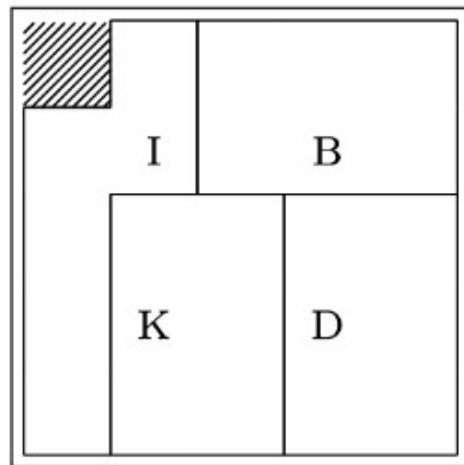
(b) 4.49%



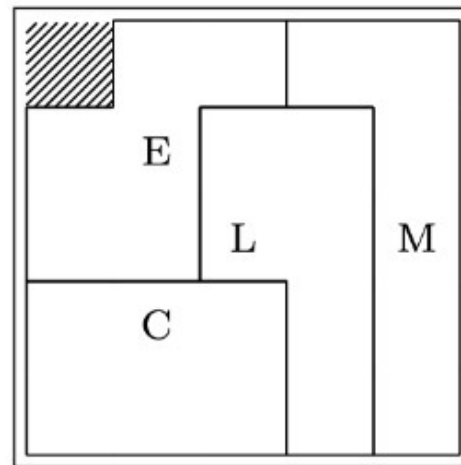
(c) 0.83%



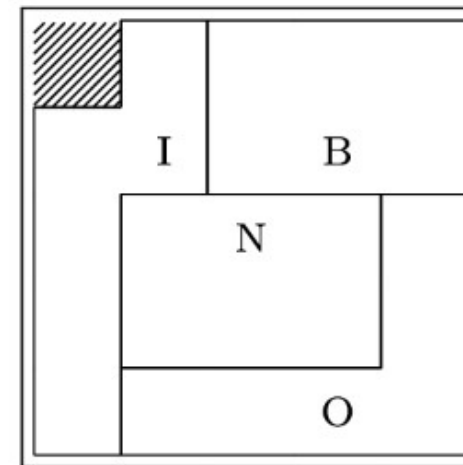
(d) 1.72%



(e) 5.18%

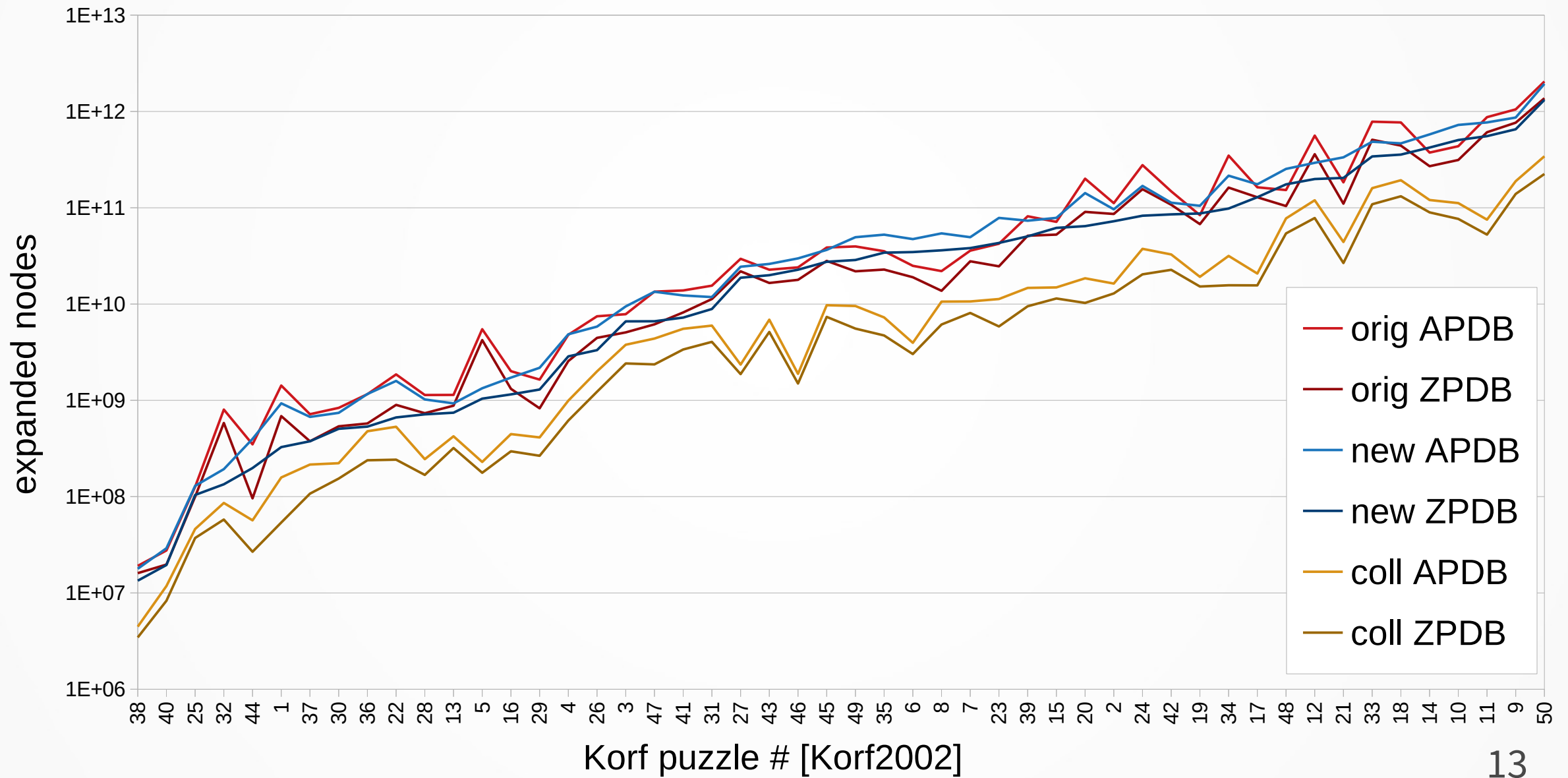


(f) 7.15%



(g) 4.77%

results



conclusions

- the zero tile can be tracked explicitly at reasonable memory and performance costs
- tracking the zero tile explicitly reduces IDA* nodes by 35%
- such PDBs can be represented with 1 bit per entry
- a small catalogue of pattern databases additionally reduces IDA* nodes by 80.2% on average